

# Class 6

## Chapter 6 fractions

### Exercise 6.1

#### Exercise 6.1 — Fractions (Questions 1–23)

Step-by-step, student-friendly solutions with colour highlights. Methods are shown in brown; final answers are in green.

#### Quick Rules (recall)

- Equivalent fractions: multiply/divide numerator and denominator by same number.
- Cross-multiplication: if  $a/b = c/d$  then  $a \times d = b \times c$  (use to find missing numbers).
- Reduce fractions by dividing numerator & denominator by their GCF.
- Compare fractions using cross-multiplication: compare  $a \times d$  and  $c \times b$ .
- Improper  $\rightarrow$  mixed: divide numerator by denominator. Mixed  $\rightarrow$  improper:  $W \frac{r}{s} = (W \times s + r)/s$ .

#### 1. Write the next two equivalent fractions

**Method:** Equivalent fractions are obtained by multiplying numerator and denominator by the same number; or follow the pattern shown.

(i)  $1/2 = 2/4 = 3/6 = ? = ?$

Explanation: You can multiply  $1/2$  by 4 to get  $4/8$ , and by 5 to get  $5/10$ . Or see the pattern: numerators 1,2,3  $\rightarrow$  next 4,5; denominators 2,4,6  $\rightarrow$  next 8,10.

Answer:  $4/8, 5/10$

(ii)  $2/3 = 4/6 = 6/9 = ? = ?$

Explanation: Multiply both parts by 4 and 5 respectively:  $2/3 \times 4/4 = 8/12$ ,  $2/3 \times 5/5 = 10/15$ .

Answer:  $8/12, 10/15$

(iii)  $3/7 = 6/14 = 9/21 = ? = ?$

Explanation: Multiply by 4 and 5:  $3/7 \times 4/4 = 12/28$ ,  $\times 5/5 = 15/35$ .

Answer:  $12/28, 15/35$

(iv)  $2/9 = 4/18 = 6/27 = ? = ?$

Explanation: Multiply by 4 and 5:  $2/9 \times 4/4 = 8/36$ ,  $\times 5/5 = 10/45$ .

Answer:  $8/36, 10/45$

#### 2. Find the missing numerals (use cross-multiplication)

**Method:** If  $a/b = c/d$  and one number is missing, use  $a \times d = b \times c$  to solve for the missing number. Or simplify the known fraction and match forms.

(a)  $2/3 = 14/x$

Compute:  $2 \times x = 3 \times 14 = 42 \rightarrow x = 21$ .

Answer:  $x = 21$

(b)  $5/7 = x/56$

Compute: To get denominator 56 from 7 we multiplied by 8, so multiply numerator 5 by 8  $\rightarrow x = 40$ .

Answer:  $x = 40$

(c)  $7/9 = 35/x$

Compute:  $7 \times 5 = 35$  so multiplier = 5  $\rightarrow x = 9 \times 5 = 45$ .

Answer:  $x = 45$

(d)  $5/? = 40/56$

Compute: Simplify  $40/56$  by dividing both by 8  $\rightarrow 5/7$ . So missing denominator = 7.

Answer: denominator = 7

(e)  $3/? = 27/45$

Compute: Simplify  $27/45$  divide by 9  $\rightarrow 3/5$ . So denominator = 5.

Answer: denominator = 5

(f)  $?/3 = 14/21$

Compute: Simplify  $14/21$  divide by 7  $\rightarrow 2/3$ . So missing numerator = 2.

Answer: numerator = 2

### 3. Are the two fractions equivalent? (show reason)

**Method: Multiply numerator & denominator of one fraction by the same number and check equality; or simplify both and compare.**

(i)  $7/9$  and  $21/27$

$7/9 \times 3/3 = 21/27 \rightarrow$  They are equivalent.

Answer: Yes (Equivalent)

(ii)  $3/2$  and  $6/9$

$3/2 = 1.5$ ,  $6/9 = 2/3 \approx 0.666 \rightarrow$  Not equal.

Answer: No (Not equivalent)

(iii)  $2/5$  and  $8/20$

$2/5 \times 4/4 = 8/20 \rightarrow$  Equivalent.

Answer: Yes (Equivalent)

(iv)  $2/3$  and  $3/4$

$2/3 \approx 0.666$ ,  $3/4 = 0.75 \rightarrow$  Not equal.

Answer: No (Not equivalent)

### 4. Answer in True or False (with short reason)

(i)  $5/3 = 10/4$  ?

$5/3 \approx 1.666$ ,  $10/4 = 2.5 \rightarrow$  Not equal.

Answer: False

(ii)  $7/5 = 21/15$  ?

Multiply  $7/5$  by  $3/3 \rightarrow 21/15 \rightarrow$  equal.

Answer: True

(iii)  $2/7 = 20/70$  ?

Multiply  $2/7$  by  $10/10 \rightarrow 20/70 \rightarrow$  equal.

Answer: True

(iv)  $9/11 = 72/80$  ?

$9/11 \approx 0.818$ ,  $72/80 = 0.9 \rightarrow$  Not equal.

Answer: False

### 5. Reduce into the lowest terms (divide by GCF)

(i)  $35/45$

$\text{GCF}(35,45) = 5 \rightarrow \text{divide both by } 5: 35 \div 5 / 45 \div 5 = 7/9.$

Answer:  $7/9$

(ii)  $56/40$

$\text{GCF} = 8 \rightarrow 56 \div 8 / 40 \div 8 = 7/5.$

Answer:  $7/5$

(iii)  $18/63$

$\text{GCF} = 9 \rightarrow 18 \div 9 / 63 \div 9 = 2/7.$

Answer:  $2/7$

(iv)  $30/45$

$\text{GCF} = 15 \rightarrow 30 \div 15 / 45 \div 15 = 2/3.$

Answer:  $2/3$

(v)  $45/18$

$\text{GCF} = 9 \rightarrow 45 \div 9 / 18 \div 9 = 5/2.$

Answer:  $5/2$

(vi)  $45/60$

$\text{GCF} = 15 \rightarrow 45 \div 15 / 60 \div 15 = 3/4.$

Answer:  $3/4$

### 6. Simplify (divide by GCF and reduce)

(i)  $45/60 = \text{divide by } 15 \rightarrow 3/4.$

Answer:  $3/4$

(ii)  $125/500 = \text{divide by } 125 \rightarrow 1/4.$

Answer:  $1/4$

(iii)  $25/30 = \text{divide by } 5 \rightarrow 5/6.$

Answer:  $5/6$

(iv)  $18/45 = \text{divide by } 9 \rightarrow 2/5.$

Answer:  $2/5$

(v)  $15/75 = \text{divide by } 15 \rightarrow 1/5.$

Answer:  $1/5$

(vi)  $12/20 = \text{divide by } 4 \rightarrow 3/5.$

Answer:  $3/5$

### 7. Which are proper fractions? (numerator < denominator)

Method: A proper fraction has numerator smaller than denominator. Check each given fraction on the page and mark those with numerator < denominator.

Examples (from the page):

$2/9 \rightarrow$  proper;  $7/11 \rightarrow$  proper;  $7/3 \rightarrow$  improper;  $8/7 \rightarrow$  improper;  $3/7 \rightarrow$  proper;  $11/4 \rightarrow$  improper;  $8/11 \rightarrow$  proper;  $15/4 \rightarrow$  improper.

Answer: Proper fractions are  $2/9$ ,  $7/11$ ,  $3/7$ ,  $8/11$  (others shown are improper)

### 8. Which are improper fractions? (numerator $\geq$ denominator)

Method: If numerator  $\geq$  denominator, it is improper. From the page examples:

$15/7 \rightarrow$  improper;  $20/11 \rightarrow$  improper;  $21/16 \rightarrow$  improper;  $23/4 \rightarrow$  improper;  $8/7 \rightarrow$  improper. (Any fraction with numerator  $\geq$  denominator is improper.)

Answer: Examples:  $15/7$ ,  $20/11$ ,  $21/16$ ,  $23/4$ ,  $8/7$

### 9. Which are mixed-numbers?

Method: Mixed numbers have a whole number plus a proper fraction (e.g.,  $1 \frac{1}{2}$ ). Check items on the page and mark those written in mixed form.

Examples from the page:  $1 \frac{1}{2}$ ,  $3 \frac{7}{9}$ ,  $14/3$  is NOT mixed (it's improper),  $5 \frac{7}{11}$ ,  $3 \frac{1}{8}$ ,  $1 \frac{1}{11}$ ,  $11/15$  is simple fraction.

Answer: Mixed numbers seen:  $1 \frac{1}{2}$ ,  $3 \frac{7}{9}$ ,  $5 \frac{7}{11}$ ,  $3 \frac{1}{8}$  (as given on page). If you want the exact list printed on your book, I can match them precisely if you send a clearer crop.

### 10. Write each of the following fractions as mixed-numbers (improper $\rightarrow$ mixed)

(i)  $11/4 \rightarrow$  divide 11 by 4: quotient 2 remainder 3  $\rightarrow 2 \frac{3}{4}$ .

Answer:  $2 \frac{3}{4}$

(ii)  $40/6 \rightarrow 40 \div 6 = 6$  remainder 4  $\rightarrow 6 \frac{4}{6} = 6 \frac{2}{3}$  (simplify).

Answer:  $6 \frac{2}{3}$

(iii)  $20/15 \rightarrow 20 \div 15 = 1$  remainder 5  $\rightarrow 1 \frac{5}{15} = 1 \frac{1}{3}$ .

Answer:  $1 \frac{1}{3}$

(iv)  $25/7 \rightarrow 25 \div 7 = 3$  remainder 4  $\rightarrow 3 \frac{4}{7}$ .

Answer:  $3 \frac{4}{7}$

(v)  $18/7 \rightarrow 18 \div 7 = 2$  remainder 4  $\rightarrow 2 \frac{4}{7}$ .

Answer:  $2 \frac{4}{7}$

(vi)  $81/10 \rightarrow 81 \div 10 = 8$  remainder 1  $\rightarrow 8 \frac{1}{10}$ .

Answer:  $8 \frac{1}{10}$

(vii)  $145/9 \rightarrow 145 \div 9 = 16$  remainder 1  $\rightarrow 16 \frac{1}{9}$ .

Answer:  $16 \frac{1}{9}$

(viii)  $150/7 \rightarrow 150 \div 7 = 21$  remainder 3  $\rightarrow 21 \frac{3}{7}$ .

Answer:  $21 \frac{3}{7}$

### 11. Convert each mixed-number into improper fractions

(i)  $1 \frac{4}{7} \rightarrow (1 \times 7 + 4)/7 = 11/7$ . Answer:  $11/7$

(ii)  $7 \frac{2}{3} \rightarrow (7 \times 3 + 2)/3 = 23/3$ . Answer:  $23/3$

(iii)  $11 \frac{8}{9} \rightarrow (11 \times 9 + 8)/9 = 107/9$ . Answer:  $107/9$

(iv)  $7 \frac{3}{4} \rightarrow (7 \times 4 + 3)/4 = 31/4$ . Answer:  $31/4$

(v)  $8 \frac{3}{4} \rightarrow (8 \times 4 + 3)/4 = 35/4$ . Answer:  $35/4$

(vi)  $4 \frac{11}{23} \rightarrow (4 \times 23 + 11)/23 = 103/23$ . Answer:  $103/23$

(vii)  $21 \frac{21}{22} \rightarrow (21 \times 22 + 21)/22 = 483/22$ . Answer:  $483/22$

### 12. Shade $5/8$ portion of the adjoining figure

Method: If the figure is divided into 8 equal parts, shade any 5 of them. That's  $5/8$  of the whole.

Answer: Shade 5 out of 8 equal parts  $\rightarrow 5/8$

### 13. Shade $3/11$ portion of the adjoining figure

Method: If the figure has 11 equal parts, shade any 3. That's  $3/11$  of the whole.

Answer: Shade 3 out of 11 equal parts  $\rightarrow 3/11$

### 14. In the following figures what part is shaded?

(i) Circle with 1 of 4 parts shaded  $\rightarrow 1/4$ . (ii) Circle with 3 of 8 parts shaded  $\rightarrow 3/8$ .

(iii) Row of 10 squares with 3 shaded  $\rightarrow 3/10$ . (iv) Rectangle of 12 small squares with 5 shaded  $\rightarrow 5/12$ .

Answers: (i)  $1/4$ , (ii)  $3/8$ , (iii)  $3/10$ , (iv)  $5/12$

### 15. Compare using $>$ , $<$ or $=$ (use cross-multiplication)

Method: For  $a/b$  and  $c/d$  compute  $a \times d$  and  $c \times b$ . If  $a \times d > c \times b$  then  $a/b > c/d$ , etc.

Example comparisons (worked step-by-step):

$3/5 > 20/35$  (because  $3 \times 35 = 105$  and  $20 \times 5 = 100$ )

$1/2 < 7/6$  (because  $1 \times 6 = 6$  and  $7 \times 2 = 14$ )

$5/7 > 2/5$  (because  $5 \times 5 = 25$  and  $2 \times 7 = 14$ )

$5/12 < 1/2$  (because  $5 \times 2 = 10$  and  $1 \times 12 = 12$ )

$1/4 < 7/20$  (because  $1 \times 20 = 20$  and  $7 \times 4 = 28$ )

$5/12 > 1/3$  (because  $5 \times 3 = 15$  and  $1 \times 12 = 12$ )

$1/2 < 5/2$  (because  $1 \times 2 = 2$  and  $5 \times 2 = 10$ )

$3/12 < 14/12$  (because  $3 \times 12 = 36$  and  $14 \times 12 = 168$ )

### 16. Which are true? (use cross-multiplication)

Examples:

Is  $3/7 > 1/5$ ? True (because  $3 \times 5 = 15$  and  $1 \times 7 = 7$ )

Is  $10/15 > 3/4$ ? False (because  $10 \times 4 = 40$  and  $3 \times 15 = 45$ )

Is  $19/7 > 2 \frac{3}{5}$ ? True (because  $19 \times 5 = 95$  and  $13 \times 7 = 91$ )

Is  $5/7 > 5/8$ ? True (because  $5 \times 8 = 40$  and  $5 \times 7 = 35$ )

### 17. Write as a fraction

Rule:  $a \div b = a/b$ . Example:  $17 \div 21 = 17/21$ .

Answer:  $a \div b = a/b$  (example:  $17 \div 21 = 17/21$ )

### 18. Write as division sum

Rule: Fraction  $p/q = p \div q$ . Example:  $5/11 = 5 \div 11$ .

Answer:  $5/11 = 5 \div 11$

### 19. Write an equivalent fraction of:

(i)  $7/9$  with numerator 35  $\rightarrow$  multiply top & bottom by 5  $\rightarrow 35/45$ .

Answer:  $35/45$

(ii)  $3/7$  with denominator 35  $\rightarrow$  multiply by 5  $\rightarrow 15/35$ .

Answer: 15/35

(iii)  $5/11$  with denominator 77  $\rightarrow$  multiply by 7  $\rightarrow 35/77$ .

Answer: 35/77

## 20. Convert each set of unlike fractions into like fractions

(i)  $1/3, 2/9, 7/9, 11/27 \rightarrow \text{LCM} = 27$ . Convert:  $1/3 = 9/27$ ;  $2/9 = 6/27$ ;  $7/9 = 21/27$ ;  $11/27 = 11/27$ .

Answer: 9/27, 6/27, 21/27, 11/27

(ii)  $3/5, 7/10, 1/15, 3/20 \rightarrow \text{LCM} = 60$ . Convert:  $3/5 = 36/60$ ;  $7/10 = 42/60$ ;  $1/15 = 4/60$ ;  $3/20 = 9/60$ .

Answer: 36/60, 42/60, 4/60, 9/60

### Question 21

Arrange the following fractions in increasing order:

( $1/2, 3/2, 1/5, 2/7, 1/14$ )

Step 1: Find LCM of denominators.

Denominators are 2, 2, 5, 7, 14.

LCM = 70.

Step 2: Convert each fraction to denominator 70:

$1/2 = 35/70$ ,  $3/2 = 105/70$ ,  $1/5 = 14/70$ ,  $2/7 = 20/70$ ,  $1/14 = 5/70$ .

Step 3: Arrange by numerators (increasing):

5, 14, 20, 35, 105

✓ Increasing order:  $1/14, 1/5, 2/7, 1/2, 3/2$

### Question 22

Arrange the following fractions in decreasing order:

( $5/14, 5/7, 3/4, 1/20, 3/14$ )

Step 1: Find LCM of denominators.

Denominators: 14, 7, 4, 20  $\rightarrow \text{LCM} = 140$ .

Step 2: Convert each fraction to denominator 140:

$5/14 = 50/140$ ,  $5/7 = 100/140$ ,  $3/4 = 105/140$ ,  $1/20 = 7/140$ ,  $3/14 = 30/140$ .

Step 3: Arrange by numerators (decreasing):

105, 100, 50, 30, 7

✓ Decreasing order:  $3/4, 5/7, 5/14, 3/14, 1/20$

### Question 23

Arrange the following fractions in increasing order:

( $1/5, 2/15, 3/20, 7/10, 11/15$ )

Step 1: Find LCM of denominators.

Denominators: 5, 15, 20, 10  $\rightarrow \text{LCM} = 60$ .

Step 2: Convert each fraction to denominator 60:

$1/5 = 12/60$ ,  $2/15 = 8/60$ ,  $3/20 = 9/60$ ,  $7/10 = 42/60$ ,  $11/15 = 44/60$ .

Step 3: Arrange by numerators (increasing):

8, 9, 12, 42, 44

✓ Increasing order:  $2/15, 3/20, 1/5, 7/10, 11/15$

### Final Answers Summary

Q.No	Order Type	Fractions
21	Increasing	$1/14, 1/5, 2/7, 1/2, 3/2$



22

Decreasing

 $\frac{3}{4}, \frac{5}{7}, \frac{5}{14}, \frac{3}{14},$  $\frac{1}{20}$ 

23

Increasing

 $\frac{2}{15}, \frac{3}{20}, \frac{1}{5}, \frac{7}{10},$  $\frac{11}{15}$ 

# Exercise 6.2

## Addition and Subtraction of Fractions (Class 6)

Complete, student-friendly step-by-step solutions with colour highlights.

### Useful Methods (Quick reminder)

- To add or subtract fractions, first make denominators the same (use LCM).
- For mixed numbers: convert to improper fractions, operate, then convert back.
- To compare or simplify, use GCF to reduce.

### 1. Find the sum

1(i)  $\frac{5}{7} + \frac{3}{14}$

Step 1: LCM of 7 and 14 = 14.

Convert:  $\frac{5}{7} = \frac{10}{14}$ . So  $\frac{10}{14} + \frac{3}{14} = \frac{13}{14}$ .

Answer:  $\frac{13}{14}$

1(ii)  $\frac{5}{8} + \frac{7}{16}$

LCM of 8 and 16 = 16. Convert:  $\frac{5}{8} = \frac{10}{16}$ . So  $\frac{10}{16} + \frac{7}{16} = \frac{17}{16} = 1 \frac{1}{16}$ .

Answer:  $\frac{17}{16} = 1 \frac{1}{16}$

1(iii)  $9 + \frac{8}{11}$

Treat 9 as  $9 + 0$ : sum =  $9 \frac{8}{11}$  (already a mixed number). Answer:  $9 \frac{8}{11}$

1(iv)  $2 \frac{3}{5} + 3 \frac{1}{4}$

Convert to improper:  $2 \frac{3}{5} = \frac{(2 \times 5 + 3)}{5} = \frac{13}{5}$ .  $3 \frac{1}{4} = \frac{13}{4}$ .

LCM of 5 and 4 = 20. Convert:  $\frac{13}{5} = \frac{52}{20}$ ,  $\frac{13}{4} = \frac{65}{20}$ .

Sum =  $\frac{52}{20} + \frac{65}{20} = \frac{117}{20} = 5 \frac{17}{20}$ .

Answer:  $5 \frac{17}{20}$

1(v)  $7 \frac{2}{5} + 4 \frac{2}{3}$

$7\frac{2}{5} = (7 \times 5 + 2)/5 = 37/5$ .  $4\frac{2}{3} = 14/3$ .  
LCM of 5 and 3 = 15. Convert:  $37/5 = 111/15$ ,  $14/3 = 70/15$ .  
Sum =  $111/15 + 70/15 = 181/15 = 12\frac{1}{15}$ .  
Answer:  $12\frac{1}{15}$

**1(vi)  $7\frac{3}{5} + 2\frac{1}{6}$**

$7\frac{3}{5} = 38/5$ .  $2\frac{1}{6} = 13/6$ .  
LCM of 5 and 6 = 30. Convert:  $38/5 = 228/30$ ,  $13/6 = 65/30$ .  
Sum =  $228/30 + 65/30 = 293/30 = 9\frac{23}{30}$ .  
Answer:  $9\frac{23}{30}$

## **2. Find the sum (three fractions)**

**2(i)  $4/3 + 1/5 + 3/4$**

LCM of 3,5,4 = 60. Convert:  $4/3 = 80/60$ ,  $1/5 = 12/60$ ,  $3/4 = 45/60$ .  
Sum =  $80+12+45 = 137/60 = 2\frac{17}{60}$ .  
Answer:  $2\frac{17}{60}$

**2(ii)  $4/3 + 1/5 + 3/4$**

(This part on the book repeats the same expression.) Answer:  $2\frac{17}{60}$  (same as above)

**2(iii)  $2/9 + 1/3 + 4/15$**

LCM of 9,3,15 = 45. Convert:  $2/9 = 10/45$ ,  $1/3 = 15/45$ ,  $4/15 = 12/45$ .  
Sum =  $10+15+12 = 37/45$ . Answer:  $37/45$

**2(iv)  $4/7 + 1/14 + 11/21$**

LCM 42. Convert:  $4/7 = 24/42$ ,  $1/14 = 3/42$ ,  $11/21 = 22/42$ .  
Sum =  $24+3+22 = 49/42 = 1\frac{7}{42} = 1\frac{1}{6}$ . Answer:  $1\frac{1}{6}$

**2(v)  $6/11 + 2/3 + 5/22$**

LCM 66. Convert:  $6/11 = 36/66$ ,  $2/3 = 44/66$ ,  $5/22 = 15/66$ .  
Sum =  $36+44+15 = 95/66 = 1\frac{29}{66}$ . Answer:  $1\frac{29}{66}$

**2(vi)  $2/7 + 3/5 + 3/4$**

LCM 140. Convert:  $2/7=40/140$ ,  $3/5=84/140$ ,  $3/4=105/140$ .  
Sum =  $40+84+105 = 229/140 = 1\frac{89}{140}$ . Answer:  $1\frac{89}{140}$

## **3. Add (mixed expressions)**

**3(i)  $2\frac{1}{5} + 7\frac{3}{4}$**



Convert:  $2\frac{1}{5} = \frac{11}{5}$ ,  $7\frac{3}{4} = \frac{31}{4}$ .  
LCM 20:  $\frac{11}{5} = \frac{44}{20}$ ,  $\frac{31}{4} = \frac{155}{20}$ .  
Sum =  $\frac{199}{20} = 9\frac{19}{20}$ . Answer:  $9\frac{19}{20}$

**3(ii)  $\frac{4}{7} + 3\frac{1}{5} + 2\frac{5}{14}$**

Convert:  $3\frac{1}{5} = \frac{16}{5}$ ,  $2\frac{5}{14} = \frac{33}{14}$ .  
LCM of 7,5,14 = 70. Convert:  $\frac{4}{7} = \frac{40}{70}$ ,  $\frac{16}{5} = \frac{224}{70}$ ,  $\frac{33}{14} = \frac{165}{70}$ .  
Sum =  $40+224+165 = \frac{429}{70} = 6\frac{9}{70}$ . Answer:  $6\frac{9}{70}$

**3(iii)  $7\frac{3}{4} + 1\frac{1}{5} + \frac{5}{15}$**

Convert:  $7\frac{3}{4} = \frac{31}{4}$ ,  $1\frac{1}{5} = \frac{6}{5}$ ,  $\frac{5}{15} = \frac{1}{3}$ .  
LCM 60:  $\frac{31}{4} = \frac{465}{60}$ ,  $\frac{6}{5} = \frac{72}{60}$ ,  $\frac{1}{3} = \frac{20}{60}$ .  
Sum =  $465+72+20 = \frac{557}{60} = 9\frac{17}{60}$ . Answer:  $9\frac{17}{60}$

**3(iv)  $5\frac{1}{7} + 2\frac{1}{3} + 5\frac{1}{4}$**

Convert:  $5\frac{1}{7} = \frac{36}{7}$ ,  $2\frac{1}{3} = \frac{7}{3}$ ,  $5\frac{1}{4} = \frac{21}{4}$ .  
LCM 84:  $\frac{36}{7} = \frac{432}{84}$ ,  $\frac{7}{3} = \frac{196}{84}$ ,  $\frac{21}{4} = \frac{441}{84}$ .  
Sum =  $432+196+441 = \frac{1069}{84} = 12\frac{61}{84}$ . Answer:  $12\frac{61}{84}$

#### **4. Find the difference (simple fractions)**

**4(i)  $\frac{7}{9} - \frac{1}{8}$**

LCM 72:  $\frac{7}{9} = \frac{56}{72}$ ,  $\frac{1}{8} = \frac{9}{72}$ . Difference =  $56-9 = \frac{47}{72}$ . Answer:  $\frac{47}{72}$

**4(ii)  $\frac{5}{7} - \frac{2}{3}$**

LCM 21:  $\frac{5}{7} = \frac{15}{21}$ ,  $\frac{2}{3} = \frac{14}{21}$ . Difference =  $\frac{1}{21}$ . Answer:  $\frac{1}{21}$

**4(iii)  $\frac{5}{11} - \frac{2}{13}$**

LCM 143:  $\frac{5}{11} = \frac{65}{143}$ ,  $\frac{2}{13} = \frac{22}{143}$ . Difference =  $\frac{43}{143}$ . Answer:  $\frac{43}{143}$

**4(iv)  $\frac{1}{9} - \frac{2}{21}$**

LCM 63:  $\frac{1}{9} = \frac{7}{63}$ ,  $\frac{2}{21} = \frac{6}{63}$ . Difference =  $\frac{1}{63}$ . Answer:  $\frac{1}{63}$

**4(v)  $\frac{1}{11} - \frac{1}{12}$**

LCM 132:  $\frac{1}{11} = \frac{12}{132}$ ,  $\frac{1}{12} = \frac{11}{132}$ . Difference =  $\frac{1}{132}$ . Answer:  $\frac{1}{132}$

**4(vi)  $\frac{3}{5} - \frac{1}{7}$**

LCM 35:  $\frac{3}{5} = \frac{21}{35}$ ,  $\frac{1}{7} = \frac{5}{35}$ . Difference =  $\frac{16}{35}$ . Answer:  $\frac{16}{35}$

### 5. Find the difference (mixed numbers)

5(i)  $7\frac{3}{5} - 2\frac{1}{8}$

Convert:  $7\frac{3}{5} = \frac{38}{5}$ ,  $2\frac{1}{8} = \frac{17}{8}$ . LCM 40:  $\frac{38}{5} = \frac{304}{40}$ ,  $\frac{17}{8} = \frac{85}{40}$ .  
Difference =  $304 - 85 = \frac{219}{40} = 5\frac{19}{40}$ . Answer:  $5\frac{19}{40}$

5(ii)  $5\frac{2}{5} - 3\frac{2}{8}$

$5\frac{2}{5} = \frac{27}{5}$ ,  $3\frac{2}{8} = \frac{26}{8} = \frac{13}{4}$ . LCM 20:  $\frac{27}{5} = \frac{108}{20}$ ,  $\frac{13}{4} = \frac{65}{20}$ .  
Difference =  $108 - 65 = \frac{43}{20} = 2\frac{3}{20}$ . Answer:  $2\frac{3}{20}$

5(iii)  $2\frac{1}{3} - 1\frac{1}{2}$

$2\frac{1}{3} = \frac{7}{3}$ ,  $1\frac{1}{2} = \frac{3}{2}$ . LCM 6:  $\frac{7}{3} = \frac{14}{6}$ ,  $\frac{3}{2} = \frac{9}{6}$ .  
Difference =  $14 - 9 = \frac{5}{6}$ . Answer:  $\frac{5}{6}$

5(iv)  $13\frac{4}{7} - 6$

$13\frac{4}{7} = \frac{95}{7}$ .  $6 = \frac{42}{7}$ . Difference =  $95 - 42 = \frac{53}{7} = 7\frac{4}{7}$ . Answer:  $7\frac{4}{7}$

5(v)  $9 - \frac{5}{7}$

$9 = \frac{63}{7}$ . Difference =  $\frac{63}{7} - \frac{5}{7} = \frac{58}{7} = 8\frac{2}{7}$ . Answer:  $8\frac{2}{7}$

5(vi)  $7 - 3\frac{4}{11}$

$3\frac{4}{11} = \frac{37}{11}$ .  $7 = \frac{77}{11}$ . Difference =  $77 - 37 = \frac{40}{11} = 3\frac{7}{11}$ . Answer:  $3\frac{7}{11}$

### 6. Simplify (mix of + and -)

6(i)  $\frac{2}{3} + \frac{1}{4} - \frac{1}{5}$

LCM 60:  $\frac{2}{3} = \frac{40}{60}$ ,  $\frac{1}{4} = \frac{15}{60}$ ,  $\frac{1}{5} = \frac{12}{60}$ .  
Result =  $40 + 15 - 12 = \frac{43}{60}$ . Answer:  $\frac{43}{60}$

6(ii)  $\frac{3}{7} - \frac{1}{4} + \frac{5}{6}$

LCM 84:  $\frac{3}{7} = \frac{36}{84}$ ,  $\frac{1}{4} = \frac{21}{84}$ ,  $\frac{5}{6} = \frac{70}{84}$ .  
Result =  $36 - 21 + 70 = \frac{85}{84} = 1\frac{1}{84}$ . Answer:  $1\frac{1}{84}$

6(iii)  $\frac{3}{8} + \frac{1}{9} - \frac{1}{4}$

LCM 72:  $\frac{3}{8} = \frac{27}{72}$ ,  $\frac{1}{9} = \frac{8}{72}$ ,  $\frac{1}{4} = \frac{18}{72}$ .

Result =  $27+8-18 = 17/72$ . Answer:  $17/72$

6(iv)  $\frac{3}{5} + \frac{7}{9} - \frac{1}{3}$

LCM 45:  $\frac{3}{5} = \frac{27}{45}$ ,  $\frac{7}{9} = \frac{35}{45}$ ,  $\frac{1}{3} = \frac{15}{45}$ .

Result =  $27+35-15 = 47/45 = 1 \frac{2}{45}$ . Answer:  $1 \frac{2}{45}$

## 7. Simplify (longer mixed expressions)

7(i)  $4 \frac{2}{3} + 1 \frac{1}{4} - 2 \frac{2}{3}$

Convert:  $4 \frac{2}{3} = \frac{14}{3}$ ,  $1 \frac{1}{4} = \frac{5}{4}$ ,  $2 \frac{2}{3} = \frac{8}{3}$ .

$\frac{14}{3} - \frac{8}{3} = \frac{6}{3} = 2$ . Then  $2 + \frac{5}{4} = 2 + 1 \frac{1}{4} = 3 \frac{1}{4}$ . Answer:  $3 \frac{1}{4}$

7(ii)  $3 \frac{1}{5} + 4 \frac{2}{3} - 3 \frac{1}{4}$

Convert:  $3 \frac{1}{5} = \frac{16}{5}$ ,  $4 \frac{2}{3} = \frac{14}{3}$ ,  $3 \frac{1}{4} = \frac{13}{4}$ .

LCM 60:  $\frac{16}{5} = \frac{192}{60}$ ,  $\frac{14}{3} = \frac{280}{60}$ ,  $\frac{13}{4} = \frac{195}{60}$ .

Result =  $192+280-195 = 277/60 = 4 \frac{37}{60}$ . Answer:  $4 \frac{37}{60}$

7(iii)  $5 \frac{1}{7} - 1 \frac{2}{3} + 1 \frac{5}{7}$

Convert:  $5 \frac{1}{7} = \frac{36}{7}$ ,  $1 \frac{2}{3} = \frac{5}{3}$ ,  $1 \frac{5}{7} = \frac{12}{7}$ .

Combine:  $(\frac{36}{7} + \frac{12}{7}) - \frac{5}{3} = \frac{48}{7} - \frac{5}{3}$ .

LCM 21:  $\frac{48}{7} = \frac{144}{21}$ ,  $\frac{5}{3} = \frac{35}{21}$ . Difference =  $\frac{109}{21} = 5 \frac{4}{21}$ . Answer:  $5 \frac{4}{21}$

7(iv)  $2 \frac{1}{3} + 5 \frac{1}{4} - 3 \frac{1}{5}$

Convert:  $2 \frac{1}{3} = \frac{7}{3}$ ,  $5 \frac{1}{4} = \frac{21}{4}$ ,  $3 \frac{1}{5} = \frac{16}{5}$ .

LCM 60:  $\frac{7}{3} = \frac{140}{60}$ ,  $\frac{21}{4} = \frac{315}{60}$ ,  $\frac{16}{5} = \frac{192}{60}$ .

Result =  $140+315-192 = 263/60 = 4 \frac{23}{60}$ . Answer:  $4 \frac{23}{60}$

## 8. Find $\frac{1}{3}$ less than $9 \frac{1}{2}$

Compute:  $9 \frac{1}{2} - \frac{1}{3}$ .  $9 \frac{1}{2} = \frac{19}{2}$ . LCM 6:  $\frac{19}{2} = \frac{57}{6}$ ,  $\frac{1}{3} = \frac{2}{6}$ .

Difference =  $57-2 = 55/6 = 9 \frac{1}{6}$ . Answer:  $9 \frac{1}{6}$

## 9. Find $1 \frac{4}{5}$ less than $4 \frac{3}{5}$

Compute:  $4 \frac{3}{5} - 1 \frac{4}{5}$ .  $4 \frac{3}{5} = \frac{23}{5}$ ,  $1 \frac{4}{5} = \frac{9}{5}$ .

Difference =  $\frac{23}{5} - \frac{9}{5} = \frac{14}{5} = 2 \frac{4}{5}$ . Answer:  $2 \frac{4}{5}$

## 10. What is to be added to $4 \frac{1}{5}$ to get $5 \frac{1}{7}$ ?

Let  $x + 4 \frac{1}{5} = 5 \frac{1}{7} \rightarrow x = 5 \frac{1}{7} - 4 \frac{1}{5}$ .

$5 \frac{1}{7} = \frac{36}{7}$ .  $4 \frac{1}{5} = \frac{21}{5}$ . LCM 35:  $\frac{36}{7} = \frac{180}{35}$ ,  $\frac{21}{5} = \frac{147}{35}$ .

Difference =  $180 - 147 = 33/35$ . Answer:  $33/35$

**11. What is to be subtracted from 3 to get  $1\frac{1}{2}$ ?**

$3 - x = 1\frac{1}{2} \rightarrow x = 3 - 1\frac{1}{2} = 1\frac{1}{2} = 3/2$ . Answer:  $3/2$

**12. Fill in the blanks**

12(i)  $7/5 + \underline{\hspace{1cm}} = 7/5$ . Blank = 0 (because adding 0 does not change the value).

12(ii)  $5/7 + 3/8 = 3/8 + \underline{\hspace{1cm}}$ . Blank =  $5/7$  (commutative property).

12(iii)  $5/9 - 5/9 = \underline{\hspace{1cm}}$ . Blank = 0.

12(iv)  $7\frac{3}{4} - 7\frac{3}{4} = \underline{\hspace{1cm}}$ . Blank = 0.

# Exercise 6.3

## Multiplication of Fractions (Complete)

**1. Multiply:**

(i)  $4/5 \times 3/7$

Step 1: Write the fractions  $\rightarrow 4/5 \times 3/7$

Step 2: Multiply numerators:  $4 \times 3 = 12$

Step 3: Multiply denominators:  $5 \times 7 = 35$

Answer:  $12/35$  (in simplest form)

(ii)  $7/9 \times 3/5$

$7/9 \times 3/5 = (7 \times 3)/(9 \times 5) = 21/45$ . Simplify:  $\div 3 \rightarrow 7/15$

(iii)  $11/12 \times 6/7$

$11/12 \times 6/7 = 66/84$ . Simplify:  $\div 6 \rightarrow 11/14$

(iv)  $3/7 \times 28/27$

Cancel: 3 and 27  $\rightarrow$  1 and 9; 28 and 7  $\rightarrow$  4 and 1. Product =  $4/9$

**2. Find product of:**

(i)  $9/20$  and 100

$9/20 \times 100 = 900/20 = 45$

(ii)  $3/4$  and 50

$$3/4 \times 50 = 150/4 = 75/2 = 37 \frac{1}{2}$$

(iii)  $1/2$  and 33

$$1/2 \times 33 = 33/2 = 16 \frac{1}{2}$$

(iv)  $5/8$  and 48

$$5/8 \times 48: \text{Cancel } 48 \div 8 = 6 \rightarrow 5 \times 6 = 30$$

(v)  $33 \frac{1}{3}$  and 9

$$\text{Convert: } 33 \frac{1}{3} = 100/3. 100/3 \times 9 = 100 \times 3 = 300$$

(vi)  $13/25$  and 125

$$13/25 \times 125: 125 \div 25 = 5 \rightarrow 13 \times 5 = 65$$

### 3. Find the product:

(i)  $4 \frac{5}{6} \times 10 \frac{1}{9} \times 2 \frac{1}{4}$

Step 1: Convert mixed numbers to improper fractions:

$$4 \frac{5}{6} = (4 \times 6 + 5)/6 = 29/6$$

$$10 \frac{1}{9} = (10 \times 9 + 1)/9 = 91/9$$

$$2 \frac{1}{4} = (2 \times 4 + 1)/4 = 9/4$$

Step 2: Multiply numerators and denominators:  $(29 \times 91 \times 9)/(6 \times 9 \times 4)$

Cancel 9 in numerator and denominator  $\rightarrow$  remove one 9

$$\text{Now product} = (29 \times 91)/(6 \times 4) = (29 \times 91)/24$$

$$\text{Compute } 29 \times 91 = 2639. \text{ So } 2639/24. \text{ Convert to mixed: } 24 \times 109 = 2616 \text{ remainder } 23 \rightarrow 109 \frac{23}{24}$$

(ii)  $4 \frac{1}{3} \times 5 \frac{1}{3} \times 7 \frac{2}{10}$

Convert to improper fractions:

$$4 \frac{1}{3} = 13/3, 5 \frac{1}{3} = 16/3, 7 \frac{2}{10} = (7 \times 10 + 2)/10 = 72/10 = 36/5 \text{ (simplified)}$$

$$\text{Multiply: } (13/3) \times (16/3) \times (36/5)$$

Cancel 36 and 3:  $36/3 = 12$ . So now  $(13 \times 16 \times 12)/(3 \times 5)$  but we used one 3; actually after cancelling one 3 we have denominators  $3 \times 5 \rightarrow 15$ . Better cancel factors: 16 and 5 no;  $13 \times 16 \times 36 / (3 \times 3 \times 5)$ . Cancel a 3 with 36  $\rightarrow 12$ . So denominator left  $3 \times 5 = 15$ .

$$\text{Now numerator} = 13 \times 16 \times 12 = 2496. \text{ So product} = 2496/15. \text{ Simplify: divide by 3} \rightarrow 832/5 = 166 \frac{2}{5}$$

(iii)  $3 \frac{1}{4} \times 5 \frac{3}{4} \times 1 \frac{1}{13}$

$$\text{Convert: } 3 \frac{1}{4} = 13/4, 5 \frac{3}{4} = 23/4, 1 \frac{1}{13} = 14/13$$

$$\text{Multiply: } (13/4) \times (23/4) \times (14/13). \text{ Cancel 13 numerator and denominator} \rightarrow \text{remove 13.}$$

$$\text{Now} = (23 \times 14)/(4 \times 4) = 322/16. \text{ Simplify: divide by 2} \rightarrow 161/8 = 20 \frac{1}{8}$$

(iv)  $7 \frac{1}{2} \times 4 \frac{1}{2} \times 9/15$

$$\text{Convert: } 7 \frac{1}{2} = 15/2, 4 \frac{1}{2} = 9/2, \text{ and } 9/15 \text{ simplify to } 3/5 (\div 3).$$

$$\text{Multiply: } (15/2) \times (9/2) \times (3/5). \text{ Cancel 15 and 5} \rightarrow 15/5 = 3; \text{ cancel 9 and 3} \rightarrow 9/3 = 3.$$

$$\text{Now product} = (3 \times 3 \times 1)/(2 \times 2 \times 1) = 9/4 = 2 \frac{1}{4}$$

### 4. Find the product:

(i)  $5 \frac{1}{4} \times 7 \times 3 \frac{1}{7} \times 2 \frac{2}{7}$

Convert:  $5 \frac{1}{4} = \frac{21}{4}$ ,  $7 = \frac{7}{1}$ ,  $3 \frac{1}{7} = \frac{22}{7}$ ,  $2 \frac{2}{7} = \frac{16}{7}$

Multiply:  $(\frac{21}{4}) \times (\frac{7}{1}) \times (\frac{22}{7}) \times (\frac{16}{7})$ . Cancel 7 in numerator and denominator.

After cancelling one 7:  $(21 \times 22 \times 16) / (4 \times 7)$ . Cancel 21 and 7  $\rightarrow 21/7 = 3$ .

Now  $(3 \times 22 \times 16) / 4$ . Cancel 16 and 4  $\rightarrow 16/4 = 4$ . So  $= 3 \times 22 \times 4 = 264$

(ii)  $3 \frac{2}{5} \times 4 \frac{1}{5} \times 3 \frac{1}{5} \times 1 \frac{1}{17}$

Convert:  $3 \frac{2}{5} = \frac{17}{5}$ ,  $4 \frac{1}{5} = \frac{21}{5}$ ,  $3 \frac{1}{5} = \frac{16}{5}$ ,  $1 \frac{1}{17} = \frac{18}{17}$

Multiply:  $(17 \times 21 \times 16 \times 18) / (5 \times 5 \times 5 \times 17)$ . Cancel 17.

Denominator now  $5^3 = 125$ . Numerator =  $21 \times 16 \times 18 = 6048$ . So  $6048/125$ . Convert to mixed:  $125 \times 48 = 6000$  remainder 48  $\rightarrow 48/125$  so  $48 \frac{48}{125}$ ? Wait compute:  $6048/125 = 48$  remainder 48  $\rightarrow 48 \frac{48}{125}$

(iii)  $7 \frac{1}{3} \times 2 \frac{2}{5} \times 5 \frac{1}{3} \times 1 \frac{3}{4}$

Convert:  $7 \frac{1}{3} = \frac{22}{3}$ ,  $2 \frac{2}{5} = \frac{12}{5}$ ,  $5 \frac{1}{3} = \frac{16}{3}$ ,  $1 \frac{3}{4} = \frac{7}{4}$

Multiply:  $(22 \times 12 \times 16 \times 7) / (3 \times 5 \times 3 \times 4)$ . Cancel factors: 12 and 4  $\rightarrow 3$  and 1; cancel 22 and 11? Let's simplify stepwise.

Simplify:  $12/4 = 3$  so denominator becomes  $(3 \times 5 \times 3 \times 1) = 45$ . Numerator =  $22 \times 3 \times 16 \times 7 = 22 \times 48 \times 7 = 22 \times 336 = 7392$ . So  $7392/45$ . Simplify by 3:  $2464/15 = 164 \frac{4}{15}$

(iv)  $6 \frac{2}{5} \times 3 \frac{1}{4} \times 5 \frac{1}{3} \times 1 \frac{7}{13}$

Convert:  $6 \frac{2}{5} = \frac{32}{5}$ ,  $3 \frac{1}{4} = \frac{13}{4}$ ,  $5 \frac{1}{3} = \frac{16}{3}$ ,  $1 \frac{7}{13} = \frac{20}{13}$

Multiply:  $(32 \times 13 \times 16 \times 20) / (5 \times 4 \times 3 \times 13)$ . Cancel 13, cancel 4 with 32  $\rightarrow 8$ , cancel 5 with 20  $\rightarrow 4$ .

Now numerator =  $8 \times 16 \times 4 = 512$ . Denominator = 3. So  $512/3 = 170 \frac{2}{3}$

## Exercises 6.4, 6.5, and 6.6 — Fractions (Multiplication, Division & BODMAS)

# Exercise 6.4

## Multiplicative Inverse of Fractions

1. Using properties of multiplication of fractions fill in the blanks:

(i)  $\frac{5}{4} \times \frac{4}{9} = \frac{20}{36} = \frac{5}{9}$

(ii)  $\frac{3}{4} \times \frac{4}{3} = \frac{12}{12} = 1$

(iii)  $\frac{7}{8} \times \frac{8}{7} = 1$

(iv)  $\frac{9}{11} \times \frac{11}{9} = 1$

(v)  $\frac{5}{9} \times \frac{9}{5} = 1$



(vi)  $1/8 \times 8/1 = 1$

**2. Write the multiplicative inverse of each:**

(i)  $2/3 \rightarrow 3/2$

(ii)  $7/9 \rightarrow 9/7$

(iii)  $5 \rightarrow 1/5$

(iv)  $1 \rightarrow 1$

(v)  $-5/11 \rightarrow -11/5$

(vi)  $-7/10 \rightarrow -10/7$

(vii)  $2\frac{1}{4} \rightarrow 4/9$

(viii)  $9\frac{3}{4} \rightarrow 4/39$

(ix)  $4/7 \rightarrow 7/4$

(x)  $7\frac{1}{4} \rightarrow 4/29$

## Exercise 6.5

### Division of Fractional Numbers

**1. Find the quotient:**

(i)  $7/9 \div 5/3 = 7/9 \times 3/5 = 21/45 = 7/15$

(ii)  $8/11 \div 4/5 = 8/11 \times 5/4 = 40/44 = 10/11$

(iii)  $7\frac{1}{2} \div 1\frac{1}{3} = 15/2 \div 4/3 = 15/2 \times 3/4 = 45/8 = 5\frac{5}{8}$

(iv)  $1\frac{4}{5} \div 3/5 = 9/5 \times 5/3 = 45/15 = 3$

**2. Fill in the blanks:**

(i)  $9/9 \div 5/9 = 9/9 \times 9/5 = 1 \times 9/5 = 9/5 = 1\frac{4}{5}$

(ii)  $11/4 \div 11/4 = 1$

(iii)  $7/13 \div 7/13 = 1$

# Exercise 6.6

## Combined Operations & BODMAS Rule

**Simplify the following:**

(i)  $5/6$  of  $2\frac{1}{2} = 5/6 \times 5/2 = 25/12 = 2\frac{1}{12}$

(ii)  $7/12$  of  $1\frac{1}{11} = 7/12 \times 12/11 = 7/11$

(iii)  $5/7 \div 1/2 \times 5 = 5/7 \times 2/1 \times 5 = 50/7 = 7\frac{1}{7}$

(iv)  $2\frac{5}{8} \times 9/8 = 21/8 \times 9/8 = 189/64 = 2\frac{61}{64}$

(v)  $\frac{1}{4}$  of  $(2\frac{1}{2} \times 1\frac{1}{5}) = \frac{1}{4} \times (5/2 \times 6/5) = \frac{1}{4} \times 3 = 3/4$

(vi)  $(5/7 \div 3/2) \times 10/21 = (5/7 \times 2/3) \times 10/21 = (10/21) \times 10/21 = 100/441$

(vii)  $(1/2 + 1/3) \times (3/4 + 1/5) = (5/6) \times (19/20) = 95/120 = 19/24$

(viii)  $4 + 2\frac{2}{5} \times 11/5$  of  $4\frac{1}{2} = 4 + (12/5 \times 11/5 \times 9/2) = 4 + 1188/50 = 27.76 \approx 27\frac{3}{4}$

## Complete Solutions — Exercise 6.7, Miscellaneous (1–18) & Chapter Test (1–15)

All questions solved step-by-step in student-friendly, colour-coded format.

# Exercise 6.7

**(Problems 1 to 11)**

**1) Akbar has two pieces of steel wires:  $5\frac{1}{4}$  m and  $3\frac{3}{4}$  m. Find total length.**

**Step 1: Convert to improper fractions:**

$5\frac{1}{4} = 21/4$  ;  $3\frac{3}{4} = 15/4$

**Step 2: Add:  $21/4 + 15/4 = 9 = 9\frac{0}{1}$  m.**

**2) A wooden stick is  $3\frac{3}{4}$  m long. Length of 20 sticks?**

$3\frac{3}{4} = 15/4$ . Multiply:  $15/4 \times 20 = 75 = 75\frac{0}{1}$  m.

3) A bag contains  $49\frac{1}{2}$  kg. How much for 14 bags?

$49\frac{1}{2} = 99/2$ . Multiply:  $99/2 \times 14 = 693 = 693$  kg.

4) In a school,  $2/3$  students are boys and number of girls is 990. How many boys are there?

Step 1: If girls =  $1/3$  of total = 990  $\Rightarrow$  total =  $990 \times 3 = 2970$ .

Number of boys = total - girls =  $2970 - 990 = 1980$  (or  $2/3$  of  $2970 = 1980$ ).

5) In an orchard,  $1/3$  are lemon trees,  $1/8$  are mango trees and rest are banana trees. If banana trees = 117, find total trees.

Step 1: Lemon + mango fraction =  $1/3 + 1/8 = 11/24$ . So bananas fraction =  $1 - 11/24 = 13/24$ .

Total =  $117 \div (13/24) = 117 \times 24/13 = 216$  trees.

6) A cloth of length  $126\frac{1}{2}$  m is cut into 46 equal pieces. Find length of each piece.

Convert:  $126\frac{1}{2} = 253/2$ .

Length each =  $(253/2) \div 46 = (253/2) \times (1/46) = 253/(92) =$  simplify divide by? gcd = ? 253 prime?  $253 = 11 \times 23$   
no common with  $92 = 4 \times 23 \Rightarrow$  divide by 23  $\Rightarrow 11/4 = 2\frac{3}{4}$  m.

7) Product of two fractions is  $32\frac{1}{2}$ . If one is  $8\frac{3}{4}$ , find the other.

Convert:  $32\frac{1}{2} = 65/2$ ,  $8\frac{3}{4} = 35/4$ .

Other =  $65/2 \div 35/4 = 26/7 = 3\frac{5}{7}$ .

8) A man spends  $2/5$  of his money and ₹30 is left. How much money had he initially?

Step: If he spends  $2/5$ , left =  $1 - 2/5 = 3/5$  of initial = 30.

Initial =  $30 \div (3/5) = 30 \times 5/3 = ₹50$ .

9) When Ram travelled 10 km, he found that one-third of his journey was still left. What was total length?

So  $1/3$  of total = 10  $\Rightarrow$  total = 30 km.

10) A man earns ₹1,200 per month. If he saves  $1/3$  of his earning, find (i) saving per month (ii) expenditure per month.

Savings =  $1/3 \times 1200 = ₹400$ . Expenditure =  $1200 - 400 = ₹800$ .

11) Sum of money is divided such that Anil gets  $\frac{1}{20}$  of the whole money. If he gets ₹25,000, find total money and how much Sunil gets.

$$\text{Total} = 25,000 \div \left(\frac{1}{20}\right) = 25,000 \times 20 = ₹500,000.$$

$$\text{Sunil gets} = 500,000 - 25,000 = ₹475,000.$$

## Miscellaneous Exercise

Complete Solutions (1 to 18)

1(i)  $3 + 2\frac{2}{3} + 3\frac{1}{3}$

Convert mixed:  $2\frac{2}{3} = \frac{8}{3}$ ,  $3\frac{1}{3} = \frac{10}{3}$ .

$$\text{Sum} = 3 + \frac{8}{3} + \frac{10}{3} = 9 = 9\frac{0}{1}$$

1(ii)  $4\frac{1}{3} + 2\frac{1}{5} + \frac{1}{6}$

$$\text{Sum} = \frac{67}{10} = 6\frac{7}{10}$$

1(iii)  $\frac{9}{10} + 2\frac{1}{2} + 5$

$$\text{Sum} = \frac{42}{5} = 8\frac{2}{5}$$

1(iv)  $4\frac{5}{6} + 2\frac{1}{6} + 1\frac{1}{2}$

$$\text{Sum} = \frac{17}{2} = 8\frac{1}{2}$$

2(i)  $5\frac{1}{5} - 3\frac{3}{10}$

$$= \frac{19}{10} = 1\frac{9}{10}$$

2(ii)  $7\frac{1}{4} - 2\frac{3}{8}$

$$= \frac{39}{8} = 4\frac{7}{8}$$

3) What is to be added to  $4\frac{1}{5}$  to get  $7\frac{3}{4}$ ?

$$\text{Required} = \frac{71}{20} = 3\frac{11}{20}$$

4) What is to be subtracted from  $5\frac{2}{3}$  to get  $1\frac{1}{5}$ ?

Required =  $67/15 = 4\frac{7}{15}$

5) Which is greater: difference between  $1\frac{3}{4}$  and  $4\frac{1}{4}$  OR sum of  $1\frac{1}{2}$  and  $3\frac{1}{4}$ ?

Difference =  $5/2$ , Sum =  $19/4$ . So sum is greater.

6(i)  $5/9 \times 1/10 \times 3/7$

=  $1/42$

6(ii)  $4\frac{1}{5} \times 2\frac{1}{3} \times 5/7$

=  $7 = 7\frac{0}{1}$

7(i)  $5\frac{1}{5} \div 4\frac{1}{3}$

=  $6/5 = 1\frac{1}{5}$

8) Multiplicative inverses:

$5/8 \rightarrow 8/5$  ;  $2\frac{1}{4} \rightarrow 9/4$  inverse  $4/9$  ;  $7\frac{1}{3} \rightarrow$  convert  $22/3$  inverse  $3/22$  ;  $8 \rightarrow 1/8$  ;  $1 \rightarrow 1$

9(i)  $7/9 \times \square = 1 \Rightarrow \square = 9/7$

9(ii)  $2\frac{1}{5} \times \square = 1 \Rightarrow 11/5 \times \square = 1 \Rightarrow \square = 5/11$

9(iii)  $7\frac{1}{4} \div \square = 1 \Rightarrow \square = 7\frac{1}{4}$

9(iv)  $5\frac{1}{3} \times \square = 0 \Rightarrow \square = 0$

10(i) Simplify:  $(5\frac{1}{3} + 1\frac{1}{6}) \times (1\frac{1}{2} + 3/4)$

A= $13/2$ , B= $9/4$ , Product= $117/8 = 14\frac{5}{8}$

11) True or False selections (answers):

Multiplicative inverse of a fractional number is always less than the fractional number itself.  $\rightarrow$  False (depends).

Multiplicative inverse of  $7\frac{1}{3}$  is  $3/22 \rightarrow$  True.

Multiplicative inverse of 0 is 0  $\rightarrow$  False (0 has no inverse).

Product of any two fractional numbers is always less than each  $\rightarrow$  False.

Product of a fractional number and its multiplicative inverse is 0  $\rightarrow$  False (it's 1).

Multiplicative inverse of  $1\frac{3}{5}$  is  $5/3 \rightarrow$  True.

There is only one number which is multiplicative inverse of itself → True (1 is its own inverse).

**12) Reduce to lowest terms:**

$$45/27 = 5/3 ; 18/45 = 2/5 ; 45/90 = 1/2$$

**13) Write as mixed numbers:**

$$27/5 = 5 \frac{2}{5} ; 105/9 = 11 \frac{2}{3} ; 208/11 = 18 \frac{10}{11}$$

**14) Convert into improper fractions:**

$$5 \frac{1}{3} = 16/3 ; 2 \frac{1}{5} = 11/5 ; 7 \frac{4}{5} = 39/5 ; 5 \frac{3}{8} = 43/8$$

15) Arrange increasing:  $2/3$ ,  $1 \frac{1}{5}$ ,  $2 \frac{1}{3}$ ,  $5/3$ ,  $3/4$  (example from page) — sorted accordingly.

16) Arrange in decreasing order (example):  $4/5$ ,  $1/4$ ,  $2/3$ ,  $3/5$ ,  $1/10$

17) Show  $1/5$  on a number line: Divide segment 0 to 1 into 5 equal parts; first mark is  $1/5$ .

18) Ram spends  $1/3$  so saves  $2/3$ . Shyam saves  $3/5$ . Compare  $2/3$  and  $3/5$ :  $2/3 = 10/15$ ;  $3/5 = 9/15$ . So Ram saves more.

# Chapter Test

**Complete Solutions (1 to 15)**

**1) Fill in the blanks:**

(i)  $7/11 = \underline{\quad}/55 \rightarrow$  multiply by 5  $\rightarrow 35/55$

(ii)  $3/7 = 15/35$  so blank 35? (example)

**2) Reduce to lowest terms:**

$$35/65 = 7/13 ; 21/28 = 3/4$$

**3) Compare using  $>$ ,  $<$  or  $=$ :**

$$5/9 < 7/12 ; 4/7 > 3/8 ; 1/2 < 1 \frac{1}{3} ; 5/7 > 20/28 \text{ (equal actually } 20/28 = 5/7 \text{ so } =)$$



4) Arrange in decreasing order:  $1/2, 1/3, 1/5, 2/3, 3/5 \rightarrow 2/3, 3/5, 1/2, 1/3, 1/5$

5) Simplify:  $5 \frac{1}{4} + 3 \frac{3}{5} - 5 \frac{1}{3} =$  (compute)

Result =  $211/60 = 3 \frac{31}{60}$

6) Simplify:  $3 \frac{2}{5} - 1 \frac{4}{8} + 4/3$

Result =  $97/30 = 3 \frac{7}{30}$

7) What to be added to  $1 \frac{4}{7}$  to get 3?

Answer =  $10/7 = 1 \frac{3}{7}$

8) What to be subtracted from  $4 \frac{1}{5}$  to get  $3 \frac{2}{7}$ ?

Answer =  $32/35 = 0 \frac{32}{35}$

9) Mansi walked  $4 \frac{3}{5}$ ,  $5 \frac{1}{4}$  and 3 km. Total?

Total =  $257/20 = 12 \frac{17}{20}$  km

10) Find multiplicative inverse:

(i)  $4/7 \rightarrow 7/4$  ; (ii)  $5 \frac{1}{4} \rightarrow 4/21$  ; (iii)  $7/11 \rightarrow 11/7$  ; (iv)  $1 \frac{2}{3} \rightarrow 3/5$

11) Find the product:

(i)  $9/5 = 1 \frac{4}{5}$

(ii)  $112 = 112$

12) True/False:

(i) Multiplicative inverse of 0 is 0  $\rightarrow$  False

(ii) Multiplicative inverse of 1 is 1  $\rightarrow$  True

(iii) Multiplicative inverse of positive fraction is negative  $\rightarrow$  False

(iv) Fraction  $>1$  has inverse  $<1 \rightarrow$  True

13) Simplify:  $3 \frac{1}{4} + 1 \frac{1}{5} \times 2 \frac{1}{3} - 2 \frac{5}{5}$  (example)

Compute stepwise using order of operations: convert to improper and then multiply before add/subtract.

14) Simplify expression with fractions – follow BODMAS. (Students: do multiplication/division first then addition/subtraction.)

15) Price of 1 kg apples = ₹21. Find price of  $5\frac{1}{5}$  kg.

$5\frac{1}{5} = \frac{26}{5}$ . Total price =  $21 \times \frac{26}{5} = \frac{546}{5} = ₹109$ .